**Appendix B**

First, a model for simulating flow-related chl*-a* (eq. (6)) was estimated from the stream gage data as the additive combination of a stationary seasonal component and serially-correlated errors:

 (B1)

 (B2)

A seasonal model of flow was estimated using linear regression for time, *T*, on an annual sinusoidal period (eq. (B1)). The residuals from this regression,  (eq. (B2)), were used to estimate the structure of the error distribution for simulating the stochastic component of flow. The error distribution was characterized using an Autoregressive Moving Average (ARMA) model to identify appropriate *p* and *q* coefficients (Hyndman and Khandakar 2008). The parameters were chosen using stepwise estimation for nonseasonal univariate time series that minimized Akaike Information Criterion (AIC). The resulting coefficients were used to generate random errors from a standard normal distribution for the length of the original time series, . These stochastic errors were multiplied by the standard deviation of the residuals in eq. (B2) (i.e.,  in eq. (6)) and added to the seasonal component in eq. (B1) to create a simulated, daily time series of the flow-component for chl*-a*, *Chlf lo* (eq. (6)).

The chl*-a* time series was created using a similar approach. The first step estimated the stationary seasonal component of the chl*-a* time series by fitting a WRTDS model (Hirsch *et al.*

2010) that explicitly included discharge from the gaged station using one year of data from the whole time series:

 (B3)

 (B4)

This approach was used to isolate an error structure for simulation that was independent of flow and biology, where the seasonal component (as time *T* on a sinusoidal annual period) was assumed to be related to biological processes. The error distribution was then estimated from the residuals (eq. (B4)) as before using an ARMA estimate of the residual parameters, *p* and *q*. Standard error estimates from the regression used at each point in the one-year time series were also retained for each residual. Errors were simulated (, eq. (7)) for the entire time series using the estimated auto-regressive structure and multiplied by the corresponding standard error estimate from the regression (, eq. (7)). The single year estimate for *Chlseas* was repeated for every year and added to the error component that covered the entire time series. All simulated errors were rescaled to the range of the original residuals that were used to estimate the distribution. Finally, the simulated flow-component, *Chlflo*, was added to the simulated biological model, *Chlbio*, to create the daily time series, *Chlobs*, in eq. (5). The final time series was then used to compare the relative abilities of WRTDS and GAMs to characterize flow-normalized trends.



FIGURE B1: Examples of simulated time series for evaluating flow-normalized results from WRTDS and GAMs. The plots show the simulated daily time series (points) and monthly samples (lines) from the daily time series used to evaluate the flow-normalized predictions. From top to bottom, the time series show the biological chl*-a* independent of flow and the three simulated datasets that represent different effects of flow: none, constant, and increasing effect. The flow-normalized results for the simulated monthly time series from each model were compared to the first time series (biological chl*-a*) that was independent of flow.